

$$\delta S = \int_{t_b}^{t_a} dt' L'(q', \dot{q}', t') - \int_{t_d}^{t_c} dt L(q, \dot{q}, t)$$