

$$= L(q, \dot{q}, t) + \frac{\delta L(q, \dot{q}, t)}{\delta q} \delta q + \frac{\delta L(q, \dot{q}, t)}{\delta \dot{q}} \delta \dot{q}$$