

$$J(q,\dot{q},t) \coloneqq I(q,\dot{q},t)\delta t + V(q,\dot{q},t) + p\delta q(t)$$