

$$= \int_{t_1}^{t_2} dt L'(q', \dot{q}', t) - \int_{t_1 + \delta t_1}^{t_2 + \delta t_2} dt L(q, \dot{q}, t)$$