

$$J(q,t) \coloneqq L(I_t q,t) \delta t + \Pi(q,t)$$