

$$L(\dot{q}, t) = \frac{1}{2} \dot{q}(t)^2$$