

$$U(T_t q, t) = \int_{\mathbb{R}} \mathrm{d}\rho \, \delta q(t + \rho) P(q, t, \rho)$$