

$$\tilde{F}_{ab} \coloneqq \partial_a \tilde{A}_b - \partial_b \tilde{A}_a - i[\tilde{A}_a, \tilde{A}_b]$$