

$$L([q],t)=q(t)\int_{\mathbb{R}}\mathrm{d}\sigma\,G(t-\sigma)q(\sigma)$$