

$$\max\{1, 2\sqrt{g}-1\} \leq \omega^2 \leq g$$