

$$L'(T_t \tilde{q}', t) = L(T_t \tilde{q}', t) + \frac{\mathrm{d}}{\mathrm{d}t} V(T_t \tilde{q}', t)$$