

$$J(T_t\tilde{q},t) \coloneqq L(T_t\tilde{q},t)\delta t(t) + V(T_t\tilde{q},t) + U(T_t\tilde{q},t)$$