

$$S(q, R) = \int_{|t| \leq R} \mathrm{d}t \, L(T_t q, t) \, , \qquad \forall R \in \mathbb{R}^+$$