

$$S(q) \coloneqq \int_{\mathbb{R}} \mathrm{d}t \, L(T_t q, t)$$