

$$E(q) := -\epsilon^{-1} J(q) = -L(q) + \int_{\mathbb{R}} \mathrm{d}\rho \, \dot{q}(\rho) P(q, \rho)$$